

# Fei on equivariant homotopy II

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Isotropy separation + Mackey functors

Need to define  $G$ -spectra briefly

Let  $V$  be a fin dim orth rep of a finite gp  $G$ .

Def An orthogonal  $G$ -spectrum  $X$  is a collection of pointed  $G$ -space  $X_V$  indexed by reps with non-equiv action of  $O(V)$ . For orthogonal inclusion  $\lambda: V \rightarrow W$  (need not be equiv) we have structure map  $\zeta^{W-\lambda V}: X_V \rightarrow X_W$  compatible with  $G$ -action and orthogonal action.  $X$  is an  $\Omega$ -spectrum if the adjoint map  $X_V \rightarrow \Omega^{W-\lambda V} X_W$  is homotopy.

Let  $Sp^G$  denote the category of  $G$ -spectra and equiv maps

Def For  $H \leq G$ ,  $\pi_k^H X = \text{colim}_{V \geq -k} \pi_{V+k}^H X_V$ .

Def A stable weak equiv is a map  $X \rightarrow Y$  in  $Sp^G$  inducing isos in  $\pi_k^H$  for all  $H \leq G$ .

There is a homotopy category  $Ho Sp^G$  in which weak equivs are isomorphisms.